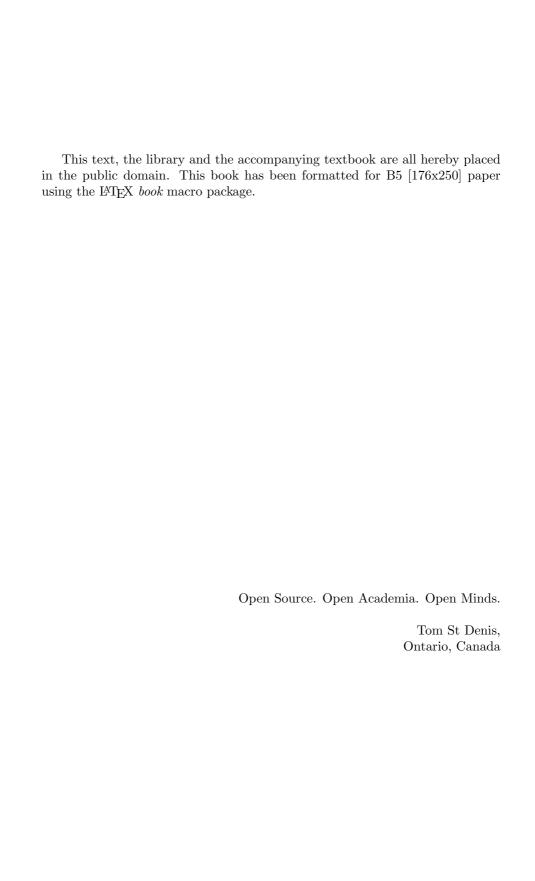
Lib Tom Math User Manual v0.32

Tom St Denis tomstdenis@iahu.ca

October 29, 2004



Contents

1	Intr	oduction 1
	1.1	What is LibTomMath?
	1.2	License
	1.3	Building LibTomMath
		1.3.1 Static Libraries
		1.3.2 Shared Libraries
		1.3.3 Testing
	1.4	Build Configuration
		1.4.1 Build Depends
		1.4.2 Build Tweaks
		1.4.3 Build Trims
	1.5	Purpose of LibTomMath
2	Get	ting Started with LibTomMath
	2.1	Building Programs
	2.2	Return Codes
	2.3	Data Types
	2.4	Function Organization
	2.5	Initialization
		2.5.1 Single Initialization
		2.5.2 Single Free
		2.5.3 Multiple Initializations
		2.5.4 Other Initializers
	2.6	Maintenance Functions
		2.6.1 Reducing Memory Usage
		2.6.2 Adding additional digits

3	Bas	ic Operations	19
	3.1	Small Constants	19
		3.1.1 Single Digit	19
		3.1.2 Long Constants	20
		3.1.3 Initialize and Setting Constants	21
	3.2	Comparisons	22
		3.2.1 Unsigned comparison	23
		3.2.2 Signed comparison	24
		3.2.3 Single Digit	25
	3.3	Logical Operations	26
		3.3.1 Multiplication by two	26
		3.3.2 Polynomial Basis Operations	28
		3.3.3 AND, OR and XOR Operations	29
	3.4	Addition and Subtraction	29
	3.5	Sign Manipulation	29
		3.5.1 Negation	29
		3.5.2 Absolute	29
	3.6	Integer Division and Remainder	30
4	Mu	Itiplication and Squaring	31
	4.1	Multiplication	31
	4.2	Squaring	33
	4.3	Tuning Polynomial Basis Routines	33
5	Mo	dular Reduction	35
	5.1	Straight Division	35
	5.2	Barrett Reduction	36
	5.3	Montgomery Reduction	37
	5.4	Restricted Dimminished Radix	40
	5.5	Unrestricted Dimminshed Radix	41
6	Exp	ponentiation	43
	6.1	Single Digit Exponentiation	43
	6.2	Modular Exponentiation	43
	6.3	Root Finding	44

7	Prin	ne Numbers	45
	7.1	Trial Division	45
	7.2	Fermat Test	45
	7.3	Miller-Rabin Test	45
		7.3.1 Required Number of Tests	46
	7.4	Primality Testing	46
	7.5	Next Prime	46
	7.6	Random Primes	47
		7.6.1 Extended Generation	47
8	Inp	ut and Output	49
	8.1	ASCII Conversions	49
		8.1.1 To ASCII	49
		8.1.2 From ASCII	49
	8.2	Binary Conversions	50
9	Alg	ebraic Functions	51
	9.1	Extended Euclidean Algorithm	51
	9.2	Greatest Common Divisor	51
	9.3	Least Common Multiple	51
	9.4	Jacobi Symbol	52
	9.5	Modular Inverse	52
	9.6	Single Digit Functions	$\frac{52}{52}$
	5.0	omerc Digit i unctions	04

List of Figures

1.1	LibTomMath Valuation	7
2.1	Return Codes	9
3.1	Comparison Codes for a, b	22
4.1	Build Names for Tuning Programs	34
7.1	Primality Generation Options	48

Chapter 1

Introduction

1.1 What is LibTomMath?

LibTomMath is a library of source code which provides a series of efficient and carefully written functions for manipulating large integer numbers. It was written in portable ISO C source code so that it will build on any platform with a conforming C compiler.

In a nutshell the library was written from scratch with verbose comments to help instruct computer science students how to implement "bignum" math. However, the resulting code has proven to be very useful. It has been used by numerous universities, commercial and open source software developers. It has been used on a variety of platforms ranging from Linux and Windows based x86 to ARM based Gameboys and PPC based MacOS machines.

1.2 License

As of the v0.25 the library source code has been placed in the public domain with every new release. As of the v0.28 release the textbook "Implementing Multiple Precision Arithmetic" has been placed in the public domain with every new release as well. This textbook is meant to compliment the project by providing a more solid walkthrough of the development algorithms used in the library.

Since both¹ are in the public domain everyone is entitled to do with them

 $^{^1\}mathrm{Note}$ that the MPI files under mtest/ are copyrighted by Michael Fromberger. They are not required to use LibTomMath.

as they see fit.

1.3 Building LibTomMath

LibTomMath is meant to be very "GCC friendly" as it comes with a makefile well suited for GCC. However, the library will also build in MSVC, Borland C out of the box. For any other ISO C compiler a makefile will have to be made by the end developer.

1.3.1 Static Libraries

To build as a static library for GCC issue the following

make

command. This will build the library and archive the object files in "libtom-math.a". Now you link against that and include "tommath.h" within your programs. Alternatively to build with MSVC issue the following

nmake -f makefile.msvc

This will build the library and archive the object files in "tommath.lib". This has been tested with MSVC version 6.00 with service pack 5.

1.3.2 Shared Libraries

To build as a shared library for GCC issue the following

make -f makefile.shared

This requires the "libtool" package (common on most Linux/BSD systems). It will build LibTomMath as both shared and static then install (by default) into /usr/lib as well as install the header files in /usr/include. The shared library (resource) will be called "libtommath.la" while the static library called "libtommath.a". Generally you use libtool to link your application against the shared object.

There is limited support for making a "DLL" in windows via the "make-file.cygwin_dll" makefile. It requires Cygwin to work with since it requires the auto-export/import functionality. The resulting DLL and import library "libtommath.dll.a" can be used to link LibTomMath dynamically to any Windows program using Cygwin.

1.3.3 Testing

To build the library and the test harness type

make test

This will build the library, "test" and "mtest/mtest". The "test" program will accept test vectors and verify the results. "mtest/mtest" will generate test vectors using the MPI library by Michael Fromberger². Simply pipe mtest into test using

mtest/mtest | test

If you do not have a "/dev/urandom" style RNG source you will have to write your own PRNG and simply pipe that into mtest. For example, if your PRNG program is called "myprng" simply invoke

myprng | mtest/mtest | test

This will output a row of numbers that are increasing. Each column is a different test (such as addition, multiplication, etc) that is being performed. The numbers represent how many times the test was invoked. If an error is detected the program will exit with a dump of the relevent numbers it was working with.

1.4 Build Configuration

LibTomMath can configured at build time in three phases we shall call "depends", "tweaks" and "trims". Each phase changes how the library is built and they are applied one after another respectively.

To make the system more powerful you can tweak the build process. Classes are defined in the file "tommath_superclass.h". By default, the symbol "LTM_ALL" shall be defined which simply instructs the system to build all of the functions. This is how LibTomMath used to be packaged. This will give you access to every function LibTomMath offers.

However, there are cases where such a build is not optional. For instance, you want to perform RSA operations. You don't need the vast majority of the library to perform these operations. Aside from LTM_ALL there is another pre–defined class "SC_RSA_1" which works in conjunction with the RSA from LibTomCrypt. Additional classes can be defined base on the need of the user.

 $^{^2\}mathrm{A}$ copy of MPI is included in the package

1.4.1 Build Depends

In the file tommath_class.h you will see a large list of C "defines" followed by a series of "ifdefs" which further define symbols. All of the symbols (technically they're macros...) represent a given C source file. For instance, BN_MP_ADD_C represents the file "bn_mp_add.c". When a define has been enabled the function in the respective file will be compiled and linked into the library. Accordingly when the define is absent the file will not be compiled and not contribute any size to the library.

You will also note that the header tommath_class.h is actually recursively included (it includes itself twice). This is to help resolve as many dependencies as possible. In the last pass the symbol LTM_LAST will be defined. This is useful for "trims".

1.4.2 Build Tweaks

A tweak is an algorithm "alternative". For example, to provide tradeoffs (usually between size and space). They can be enabled at any pass of the configuration phase.

Define	Purpose
BN_MP_DIV_SMALL	Enables a slower, smaller and equally
	functional mp_div() function

1.4.3 Build Trims

A trim is a manner of removing functionality from a function that is not required. For instance, to perform RSA cryptography you only require exponentiation with odd moduli so even moduli support can be safely removed. Build trims are meant to be defined on the last pass of the configuration which means they are to be defined only if LTM_LAST has been defined.

Moduli Related

Restriction	Undefine
Exponentiation with odd moduli only	BN_S_MP_EXPTMOD_C
	BN_MP_REDUCE_C
	BN_MP_REDUCE_SETUP_C
	BN_S_MP_MUL_HIGH_DIGS_C
	BN_FAST_S_MP_MUL_HIGH_DIGS_C
Exponentiation with random odd moduli	(The above plus the following)
	BN_MP_REDUCE_2K_C
	BN_MP_REDUCE_2K_SETUP_C
	BN_MP_REDUCE_IS_2K_C
	BN_MP_DR_IS_MODULUS_C
	BN_MP_DR_REDUCE_C
	BN_MP_DR_SETUP_C
Modular inverse odd moduli only	BN_MP_INVMOD_SLOW_C
Modular inverse (both, smaller/slower)	BN_FAST_MP_INVMOD_C

Operand Size Related

Restriction	Undefine
$Moduli \le 2560 bits$	BN_MP_MONTGOMERY_REDUCE_C
	BN_S_MP_MUL_DIGS_C
	BN_S_MP_MUL_HIGH_DIGS_C
	BN_S_MP_SQR_C
Polynomial Schmolynomial	BN_MP_KARATSUBA_MUL_C
	BN_MP_KARATSUBA_SQR_C
	BN_MP_TOOM_MUL_C
	BN_MP_TOOM_SQR_C

1.5 Purpose of LibTomMath

Unlike GNU MP (GMP) Library, LIP, OpenSSL or various other commercial kits (Miracl), LibTomMath was not written with bleeding edge performance in mind. First and foremost LibTomMath was written to be entirely open. Not only is the source code public domain (unlike various other GPL/etc licensed code), not only is the code freely downloadable but the source code is also accessible for computer science students attempting to learn "BigNum" or multiple precision arithmetic techniques.

LibTomMath was written to be an instructive collection of source code. This is why there are many comments, only one function per source file and often I use a "middle-road" approach where I don't cut corners for an extra 2% speed increase.

Source code alone cannot really teach how the algorithms work which is why I also wrote a textbook that accompanies the library (beat that!).

So you may be thinking "should I use LibTomMath?" and the answer is a definite maybe. Let me tabulate what I think are the pros and cons of LibTomMath by comparing it to the math routines from GnuPG³.

 $^{^3}$ GnuPG v1.2.3 versus LibTomMath v0.28

Criteria	Pro	Con	Notes
Few lines of code per file	X		GnuPG = 300.9, $LibTomMath = 76.04$
Commented function prototypes	X		GnuPG function names are cryptic.
Speed		X	LibTomMath is slower.
Totally free	X		GPL has unfavourable restrictions.
Large function base	X		GnuPG is barebones.
Four modular reduction algorithms	X		Faster modular exponentiation.
Portable	X		GnuPG requires configuration to build.

Figure 1.1: LibTomMath Valuation

It may seem odd to compare LibTomMath to GnuPG since the math in GnuPG is only a small portion of the entire application. However, LibTomMath was written with cryptography in mind. It provides essentially all of the functions a cryptosystem would require when working with large integers.

So it may feel tempting to just rip the math code out of GnuPG (or GnuMP where it was taken from originally) in your own application but I think there are reasons not to. While LibTomMath is slower than libraries such as GnuMP it is not normally significantly slower. On x86 machines the difference is normally a factor of two when performing modular exponentiations.

Essentially the only time you wouldn't use LibTomMath is when blazing speed is the primary concern.

Chapter 2

Getting Started with LibTomMath

2.1 Building Programs

In order to use LibTomMath you must include "tommath.h" and link against the appropriate library file (typically libtommath.a). There is no library initialization required and the entire library is thread safe.

2.2 Return Codes

There are three possible return codes a function may return.

Code	Meaning	
MP_OKAY	The function succeeded.	
MP_VAL	The function input was invalid.	
MP_MEM	Heap memory exhausted.	
MP_YES	Response is yes.	
MP_NO	Response is no.	

Figure 2.1: Return Codes

The last two codes listed are not actually "return'ed" by a function. They

are placed in an integer (the caller must provide the address of an integer it can store to) which the caller can access. To convert one of the three return codes to a string use the following function.

```
char *mp_error_to_string(int code);
```

This will return a pointer to a string which describes the given error code. It will not work for the return codes MP_YES and MP_NO.

2.3 Data Types

The basic "multiple precision integer" type is known as the "mp_int" within LibTomMath. This data type is used to organize all of the data required to manipulate the integer it represents. Within LibTomMath it has been prototyped as the following.

```
typedef struct {
    int used, alloc, sign;
    mp_digit *dp;
} mp_int;
```

Where "mp_digit" is a data type that represents individual digits of the integer. By default, an mp_digit is the ISO C "unsigned long" data type and each digit is 28—bits long. The mp_digit type can be configured to suit other platforms by defining the appropriate macros.

All LTM functions that use the mp_int type will expect a pointer to mp_int structure. You must allocate memory to hold the structure itself by yourself (whether off stack or heap it doesn't matter). The very first thing that must be done to use an mp_int is that it must be initialized.

2.4 Function Organization

The arithmetic functions of the library are all organized to have the same style prototype. That is source operands are passed on the left and the destination is on the right. For instance,

Another feature of the way the functions have been implemented is that source operands can be destination operands as well. For instance,

This allows operands to be re-used which can make programming simpler.

2.5 Initialization

2.5.1 Single Initialization

A single mp_int can be initialized with the "mp_init" function.

```
int mp_init (mp_int * a);
```

This function expects a pointer to an mp_int structure and will initialize the members of the structure so the mp_int represents the default integer which is zero. If the functions returns MP_OKAY then the mp_int is ready to be used by the other LibTomMath functions.

2.5.2 Single Free

When you are finished with an mp_int it is ideal to return the heap it used back to the system. The following function provides this functionality.

```
void mp_clear (mp_int * a);
```

The function expects a pointer to a previously initialized mp_int structure and frees the heap it uses. It sets the pointer¹ within the mp_int to **NULL** which is used to prevent double free situations. Is is legal to call mp_clear() twice on the same mp_int in a row.

2.5.3 Multiple Initializations

Certain algorithms require more than one large integer. In these instances it is ideal to initialize all of the mp_int variables in an "all or nothing" fashion. That is, they are either all initialized successfully or they are all not initialized.

The mp_init_multi() function provides this functionality.

```
int mp_init_multi(mp_int *mp, ...);
```

It accepts a **NULL** terminated list of pointers to mp_int structures. It will attempt to initialize them all at once. If the function returns MP_OKAY then all of the mp_int variables are ready to use, otherwise none of them are available for use. A complementary mp_clear_multi() function allows multiple mp_int variables to be free'd from the heap at the same time.

 $^{^{1}\}mathrm{The}$ "dp" member.

2.5.4 Other Initializers

To initialized and make a copy of an mp_int the mp_init_copy() function has been provided.

```
}
/* now num2 is ready and contains a copy of num1 */
/* We're done with them. */
mp_clear_multi(&num1, &num2, NULL);
return EXIT_SUCCESS;
}
```

Another less common initializer is mp_init_size() which allows the user to initialize an mp_int with a given default number of digits. By default, all initializers allocate MP_PREC digits. This function lets you override this behaviour.

```
int mp_init_size (mp_int * a, int size);
```

The size parameter must be greater than zero. If the function succeeds the mp_int a will be initialized to have size digits (which are all initially zero).

2.6 Maintenance Functions

2.6.1 Reducing Memory Usage

When an mp_int is in a state where it won't be changed again² excess digits can be removed to return memory to the heap with the mp_shrink() function.

```
int mp_shrink (mp_int * a);
```

This will remove excess digits of the mp_int a. If the operation fails the mp_int should be intact without the excess digits being removed. Note that you can use a shrunk mp_int in further computations, however, such operations will require heap operations which can be slow. It is not ideal to shrink mp_int variables that you will further modify in the system (unless you are seriously low on memory).

```
int main(void)
  mp_int number;
  int result;
  if ((result = mp_init(&number)) != MP_OKAY) {
     printf("Error initializing the number. %s",
            mp_error_to_string(result));
     return EXIT_FAILURE;
  }
  /* use the number [e.g. pre-computation] */
  /* We're done with it for now. */
  if ((result = mp_shrink(&number)) != MP_OKAY) {
     printf("Error shrinking the number.
             mp_error_to_string(result));
     return EXIT_FAILURE;
   }
  /* use it .... */
  /* we're done with it. */
```

²A Diffie-Hellman modulus for instance.

```
mp_clear(&number);
return EXIT_SUCCESS;
}
```

2.6.2 Adding additional digits

Within the mp_int structure are two parameters which control the limitations of the array of digits that represent the integer the mp_int is meant to equal. The *used* parameter dictates how many digits are significant, that is, contribute to the value of the mp_int. The *alloc* parameter dictates how many digits are currently available in the array. If you need to perform an operation that requires more digits you will have to mp_grow() the mp_int to your desired size.

```
int mp_grow (mp_int * a, int size);
```

This will grow the array of digits of a to size. If the *alloc* parameter is already bigger than size the function will not do anything.

```
/* we're done with it. */
mp_clear(&number);

return EXIT_SUCCESS;
}
```

Chapter 3

Basic Operations

3.1 Small Constants

Setting mp_ints to small constants is a relatively common operation. To accomodate these instances there are two small constant assignment functions. The first function is used to set a single digit constant while the second sets an ISO C style "unsigned long" constant. The reason for both functions is efficiency. Setting a single digit is quick but the domain of a digit can change (it's always at least 0...127).

3.1.1 Single Digit

Setting a single digit can be accomplished with the following function.

```
void mp_set (mp_int * a, mp_digit b);
```

This will zero the contents of a and make it represent an integer equal to the value of b. Note that this function has a return type of **void**. It cannot cause an error so it is safe to assume the function succeeded.

```
int main(void)
{
    mp_int number;
    int result;

if ((result = mp_init(&number)) != MP_OKAY) {
```

3.1.2 Long Constants

To set a constant that is the size of an ISO C "unsigned long" and larger than a single digit the following function can be used.

```
int mp_set_int (mp_int * a, unsigned long b);
```

This will assign the value of the 32-bit variable b to the mp_int a. Unlike mp_set() this function will always accept a 32-bit input regardless of the size of a single digit. However, since the value may span several digits this function can fail if it runs out of heap memory.

To get the "unsigned long" copy of an mp_int the following function can be used.

This should output the following if the program succeeds.

number == 654321

3.1.3 Initialize and Setting Constants

To both initialize and set small constants the following two functions are available.

```
int mp_init_set (mp_int * a, mp_digit b);
int mp_init_set_int (mp_int * a, unsigned long b);
```

Both functions work like the previous counterparts except they first mp_init a before setting the values.

3.2 Comparisons

Number1, Number2 == 100, 1023

Comparisons in LibTomMath are always performed in a "left to right" fashion. There are three possible return codes for any comparison.

Result Code	Meaning
MP_GT	a > b
MP_EQ	a = b
MP_LT	a < b

Figure 3.1: Comparison Codes for a, b

In figure 3.1 two integers a and b are being compared. In this case a is said to be "to the left" of b.

3.2.1 Unsigned comparison

An unsigned comparison considers only the digits themselves and not the associated *sign* flag of the mp_int structures. This is analogous to an absolute comparison. The function mp_cmp_mag() will compare two mp_int variables based on their digits only.

```
int mp_cmp(mp_int * a, mp_int * b);
```

This will compare a to b placing a to the left of b. This function cannot fail and will return one of the three compare codes listed in figure 3.1.

```
int main(void)
  mp_int number1, number2;
  int result;
  if ((result = mp_init_multi(&number1, &number2, NULL)) != MP_OKAY) {
     printf("Error initializing the numbers. %s",
             mp_error_to_string(result));
     return EXIT_FAILURE;
  }
  /* set the number1 to 5 */
  mp_set(&number1, 5);
  /* set the number2 to -6 */
  mp_set(&number2, 6);
  if ((result = mp_neg(&number2, &number2)) != MP_OKAY) {
     printf("Error negating number2. %s",
             mp_error_to_string(result));
     return EXIT_FAILURE;
  switch(mp_cmp_mag(&number1, &number2)) {
       case MP_GT: printf("|number1| > |number2|"); break;
      case MP_EQ: printf("|number1| = |number2|"); break;
       case MP_LT: printf("|number1| < |number2|"); break;</pre>
  /* we're done with it. */
  mp_clear_multi(&number1, &number2, NULL);
```

```
return EXIT_SUCCESS; } 
 If this program completes successfully it should print the following. |\texttt{number1}| < |\texttt{number2}| This is because |-6| = 6 and obviously 5 < 6.
```

3.2.2 Signed comparison

To compare two mp_int variables based on their signed value the mp_cmp() function is provided.

```
int mp_cmp(mp_int * a, mp_int * b);
```

This will compare a to the left of b. It will first compare the signs of the two mp_int variables. If they differ it will return immediately based on their signs. If the signs are equal then it will compare the digits individually. This function will return one of the compare conditions codes listed in figure 3.1.

¹This function uses the mp_neg() function which is discussed in section 3.5.1.

3.2. COMPARISONS

25

```
mp_error_to_string(result));
  return EXIT_FAILURE;
}

switch(mp_cmp(&number1, &number2)) {
    case MP_GT: printf("number1 > number2"); break;
    case MP_EQ: printf("number1 = number2"); break;
    case MP_LT: printf("number1 < number2"); break;
}

/* we're done with it. */
  mp_clear_multi(&number1, &number2, NULL);
  return EXIT_SUCCESS;
}</pre>
```

If this program² completes successfully it should print the following.

number1 > number2

3.2.3 Single Digit

To compare a single digit against an mp_int the following function has been provided.

```
int mp_cmp_d(mp_int * a, mp_digit b);
```

This will compare a to the left of b using a signed comparison. Note that it will always treat b as positive. This function is rather handy when you have to compare against small values such as 1 (which often comes up in cryptography). The function cannot fail and will return one of the tree compare condition codes listed in figure 3.1.

```
int main(void)
{
    mp_int number;
    int result;

if ((result = mp_init(&number)) != MP_OKAY) {
        printf("Error initializing the number. %s",
```

²This function uses the mp_neg() function which is discussed in section 3.5.1.

```
mp_error_to_string(result));
  return EXIT_FAILURE;
}

/* set the number to 5 */
  mp_set(&number, 5);

switch(mp_cmp_d(&number, 7)) {
    case MP_GT: printf("number > 7"); break;
    case MP_EQ: printf("number = 7"); break;
    case MP_LT: printf("number < 7"); break;
}

/* we're done with it. */
  mp_clear(&number);

return EXIT_SUCCESS;
}</pre>
```

If this program functions properly it will print out the following.

number < 7

3.3 Logical Operations

Logical operations are operations that can be performed either with simple shifts or boolean operators such as AND, XOR and OR directly. These operations are very quick.

3.3.1 Multiplication by two

Multiplications and divisions by any power of two can be performed with quick logical shifts either left or right depending on the operation.

When multiplying or dividing by two a special case routine can be used which are as follows.

```
int mp_mul_2(mp_int * a, mp_int * b);
int mp_div_2(mp_int * a, mp_int * b);
```

The former will assign twice a to b while the latter will assign half a to b. These functions are fast since the shift counts and maskes are hardcoded into the routines.

```
int main(void)
  mp_int number;
  int result;
  if ((result = mp_init(&number)) != MP_OKAY) {
     printf("Error initializing the number. %s",
             mp_error_to_string(result));
     return EXIT_FAILURE;
  }
  /* set the number to 5 */
  mp_set(&number, 5);
  /* multiply by two */
  if ((result = mp_mul_2(&number, &number)) != MP_OKAY) {
      printf("Error multiplying the number. %s",
             mp_error_to_string(result));
     return EXIT_FAILURE;
  switch(mp_cmp_d(&number, 7)) {
       case MP_GT: printf("2*number > 7"); break;
       case MP_EQ: printf("2*number = 7"); break;
      case MP_LT: printf("2*number < 7"); break;</pre>
  }
  /* now divide by two */
  if ((result = mp_div_2(&number, &number)) != MP_OKAY) {
     printf("Error dividing the number. %s",
             mp_error_to_string(result));
     return EXIT_FAILURE;
  switch(mp_cmp_d(&number, 7)) {
       case MP_GT: printf("2*number/2 > 7"); break;
       case MP_EQ: printf("2*number/2 = 7"); break;
       case MP_LT: printf("2*number/2 < 7"); break;</pre>
  }
  /* we're done with it. */
  mp_clear(&number);
  return EXIT_SUCCESS;
```

}

If this program is successful it will print out the following text.

```
2*number > 7
2*number/2 < 7
```

Since 10 > 7 and 5 < 7. To multiply by a power of two the following function can be used.

```
int mp_mul_2d(mp_int * a, int b, mp_int * c);
```

This will multiply a by 2^b and store the result in "c". If the value of b is less than or equal to zero the function will copy a to "c" without performing any further actions.

To divide by a power of two use the following.

```
int mp_div_2d (mp_int * a, int b, mp_int * c, mp_int * d);
```

Which will divide a by 2^b , store the quotient in "c" and the remainder in "d". If $b \leq 0$ then the function simply copies a over to "c" and zeroes d. The variable d may be passed as a **NULL** value to signal that the remainder is not desired.

3.3.2 Polynomial Basis Operations

Strictly speaking the organization of the integers within the mp_int structures is what is known as a "polynomial basis". This simply means a field element is stored by divisions of a radix. For example, if $f(x) = \sum_{i=0}^{k} y_i x^k$ for any vector \vec{y} then the array of digits in \vec{y} are said to be the polynomial basis representation of z if $f(\beta) = z$ for a given radix β .

To multiply by the polynomial g(x) = x all you have todo is shift the digits of the basis left one place. The following function provides this operation.

```
int mp_lshd (mp_int * a, int b);
```

This will multiply a in place by x^b which is equivalent to shifting the digits left b places and inserting zeroes in the least significant digits. Similarly to divide by a power of x the following function is provided.

```
void mp_rshd (mp_int * a, int b)
```

This will divide a in place by x^b and discard the remainder. This function cannot fail as it performs the operations in place and no new digits are required to complete it.

3.3.3 AND, OR and XOR Operations

While AND, OR and XOR operations are not typical "bignum functions" they can be useful in several instances. The three functions are prototyped as follows.

```
int mp_or (mp_int * a, mp_int * b, mp_int * c);
int mp_and (mp_int * a, mp_int * b, mp_int * c);
int mp_xor (mp_int * a, mp_int * b, mp_int * c);
```

Which compute $c = a \odot b$ where \odot is one of OR, AND or XOR.

3.4 Addition and Subtraction

To compute an addition or subtraction the following two functions can be used.

```
int mp_add (mp_int * a, mp_int * b, mp_int * c);
int mp_sub (mp_int * a, mp_int * b, mp_int * c)
```

Which perform $c=a\odot b$ where \odot is one of signed addition or subtraction. The operations are fully sign aware.

3.5 Sign Manipulation

3.5.1 Negation

Simple integer negation can be performed with the following.

```
int mp_neg (mp_int * a, mp_int * b);
```

Which assigns -a to b.

3.5.2 Absolute

Simple integer absolutes can be performed with the following.

```
int mp_abs (mp_int * a, mp_int * b);
```

Which assigns |a| to b.

3.6 Integer Division and Remainder

To perform a complete and general integer division with remainder use the following function.

```
int mp_div (mp_int * a, mp_int * b, mp_int * c, mp_int * d);
```

This divides a by b and stores the quotient in c and d. The signed quotient is computed such that bc + d = a. Note that either of c or d can be set to **NULL** if their value is not required. If b is zero the function returns \mathbf{MP} - \mathbf{VAL} .

Multiplication and Squaring

4.1 Multiplication

A full signed integer multiplication can be performed with the following.

```
int mp_mul (mp_int * a, mp_int * b, mp_int * c);
```

Which assigns the full signed product ab to c. This function actually breaks into one of four cases which are specific multiplication routines optimized for given parameters. First there are the Toom-Cook multiplications which should only be used with very large inputs. This is followed by the Karatsuba multiplications which are for moderate sized inputs. Then followed by the Comba and baseline multipliers.

Fortunately for the developer you don't really need to know this unless you really want to fine tune the system. mp_mul() will determine on its own¹ what routine to use automatically when it is called.

```
int main(void)
{
   mp_int number1, number2;
   int result;

/* Initialize the numbers */
   if ((result = mp_init_multi(&number1,
```

 $^{^{1}\}mathrm{Some}$ tweaking may be required.

```
&number2, NULL)) != MP_OKAY) {
      printf("Error initializing the numbers. %s",
             mp_error_to_string(result));
      return EXIT_FAILURE;
   /* set the terms */
   if ((result = mp_set_int(&number, 257)) != MP_OKAY) {
      printf("Error setting number1. %s",
             mp_error_to_string(result));
      return EXIT_FAILURE;
   }
   if ((result = mp_set_int(&number2, 1023)) != MP_OKAY) {
      printf("Error setting number2. %s",
             mp_error_to_string(result));
      return EXIT_FAILURE;
   /* multiply them */
   if ((result = mp_mul(&number1, &number2,
                        &number1)) != MP_OKAY) {
      printf("Error multiplying terms. %s",
             mp_error_to_string(result));
      return EXIT_FAILURE;
   /* display */
   printf("number1 * number2 == %lu", mp_get_int(&number1));
   /* free terms and return */
   mp_clear_multi(&number1, &number2, NULL);
   return EXIT_SUCCESS;
   If this program succeeds it shall output the following.
number1 * number2 == 262911
```

4.2 Squaring

Since squaring can be performed faster than multiplication it is performed it's own function instead of just using mp_mul().

```
int mp_sqr (mp_int * a, mp_int * b);
```

Will square a and store it in b. Like the case of multiplication there are four different squaring algorithms all which can be called from mp_sqr(). It is ideal to use mp_sqr over mp_mul when squaring terms.

4.3 Tuning Polynomial Basis Routines

Both of the Toom-Cook and Karatsuba multiplication algorithms are faster than the traditional $O(n^2)$ approach that the Comba and baseline algorithms use. At $O(n^{1.464973})$ and $O(n^{1.584962})$ running times respectfully they require considerably less work. For example, a 10000-digit multiplication would take roughly 724,000 single precision multiplications with Toom-Cook or 100,000,000 single precision multiplications with the standard Comba (a factor of 138).

So why not always use Karatsuba or Toom-Cook? The simple answer is that they have so much overhead that they're not actually faster than Comba until you hit distinct "cutoff" points. For Karatsuba with the default configuration, GCC 3.3.1 and an Athlon XP processor the cutoff point is roughly 110 digits (about 70 for the Intel P4). That is, at 110 digits Karatsuba and Comba multiplications just about break even and for 110+ digits Karatsuba is faster.

Toom-Cook has incredible overhead and is probably only useful for very large inputs. So far no known cutoff points exist and for the most part I just set the cutoff points very high to make sure they're not called.

A demo program in the "etc/" directory of the project called "tune.c" can be used to find the cutoff points. This can be built with GCC as follows

make XXX

Where "XXX" is one of the following entries from the table 4.1.

When the program is running it will output a series of measurements for different cutoff points. It will first find good Karatsuba squaring and multiplication points. Then it proceeds to find Toom-Cook points. Note that the Toom-Cook tuning takes a very long time as the cutoff points are likely to be very high.

Value of XXX	Meaning
tune	Builds portable tuning application
tune86	Builds x86 (pentium and up) program for COFF
tune86c	Builds x86 program for Cygwin
tune86l	Builds x86 program for Linux (ELF format)

Figure 4.1: Build Names for Tuning Programs

Modular Reduction

Modular reduction is process of taking the remainder of one quantity divided by another. Expressed as (5.1) the modular reduction is equivalent to the remainder of b divided by c.

$$a \equiv b \pmod{c} \tag{5.1}$$

Of particular interest to cryptography are reductions where b is limited to the range $0 \le b < c^2$ since particularly fast reduction algorithms can be written for the limited range.

Note that one of the four optimized reduction algorithms are automatically chosen in the modular exponentiation algorithm mp_exptmod when an appropriate modulus is detected.

5.1 Straight Division

In order to effect an arbitrary modular reduction the following algorithm is provided.

```
int mp_mod(mp_int *a, mp_int *b, mp_int *c);
```

This reduces a modulo b and stores the result in c. The sign of c shall agree with the sign of b. This algorithm accepts an input a of any range and is not limited by $0 \le a < b^2$.

5.2 Barrett Reduction

Barrett reduction is a generic optimized reduction algorithm that requires precomputation to achieve a decent speedup over straight division. First a mu value must be precomputed with the following function.

```
int mp_reduce_setup(mp_int *a, mp_int *b);
```

Given a modulus in b this produces the required mu value in a. For any given modulus this only has to be computed once. Modular reduction can now be performed with the following.

```
int mp_reduce(mp_int *a, mp_int *b, mp_int *c);
```

This will reduce a in place modulo b with the precomputed mu value in c. a must be in the range $0 \le a < b^2$.

```
int main(void)
            a, b, c, mu;
  mp_int
   int
            result;
   /* initialize a,b to desired values, mp_init mu,
    * c and set c to 1...we want to compute a^3 mod b
    */
   /* get mu value */
   if ((result = mp_reduce_setup(&mu, b)) != MP_OKAY) {
      printf("Error getting mu.
             mp_error_to_string(result));
      return EXIT_FAILURE;
   }
   /* square a to get c = a^2 */
   if ((result = mp_sqr(&a, &c)) != MP_OKAY) {
      printf("Error squaring. %s",
             mp_error_to_string(result));
      return EXIT_FAILURE;
   }
```

```
/* now reduce 'c' modulo b */
   if ((result = mp_reduce(&c, &b, &mu)) != MP_OKAY) {
     printf("Error reducing. %s",
             mp_error_to_string(result));
     return EXIT_FAILURE;
   }
  /* multiply a to get c = a^3 */
  if ((result = mp_mul(&a, &c, &c)) != MP_OKAY) {
     printf("Error reducing. %s",
             mp_error_to_string(result));
     return EXIT_FAILURE;
   /* now reduce 'c' modulo b */
   if ((result = mp_reduce(&c, &b, &mu)) != MP_OKAY) {
     printf("Error reducing. %s",
             mp_error_to_string(result));
     return EXIT_FAILURE;
   }
  /* c now equals a^3 mod b */
  return EXIT_SUCCESS;
}
```

This program will calculate $a^3 \mod b$ if all the functions succeed.

5.3 Montgomery Reduction

Montgomery is a specialized reduction algorithm for any odd moduli. Like Barrett reduction a pre–computation step is required. This is accomplished with the following.

```
int mp_montgomery_setup(mp_int *a, mp_digit *mp);
```

For the given odd moduli a the precomputation value is placed in mp. The reduction is computed with the following.

```
int mp_montgomery_reduce(mp_int *a, mp_int *m, mp_digit mp);
```

This reduces a in place modulo m with the pre–computed value mp. a must be in the range $0 \le a < b^2$.

Montgomery reduction is faster than Barrett reduction for moduli smaller than the "comba" limit. With the default setup for instance, the limit is 127 digits (3556-bits). Note that this function is not limited to 127 digits just that it falls back to a baseline algorithm after that point.

An important observation is that this reduction does not return $a \mod m$ but $aR^{-1} \mod m$ where $R = \beta^n$, n is the n number of digits in m and β is radix used (default is 2^{28}).

To quickly calculate R the following function was provided.

```
int mp_montgomery_calc_normalization(mp_int *a, mp_int *b);
```

Which calculates a=R for the odd moduli b without using multiplication or division.

The normal modus operandi for Montgomery reductions is to normalize the integers before entering the system. For example, to calculate $a^3 \mod b$ using Montgomery reduction the value of a can be normalized by multiplying it by R. Consider the following code snippet.

```
int main(void)
  mp_int
            a, b, c, R;
  mp_digit mp;
   int
            result;
   /* initialize a,b to desired values,
    * mp_init R, c and set c to 1....
    */
   /* get normalization */
   if ((result = mp_montgomery_calc_normalization(&R, b)) != MP_OKAY) {
      printf("Error getting norm. %s",
             mp_error_to_string(result));
      return EXIT_FAILURE;
   }
   /* get mp value */
   if ((result = mp_montgomery_setup(&c, &mp)) != MP_OKAY) {
```

```
printf("Error setting up montgomery.
                                         %s",
          mp_error_to_string(result));
  return EXIT_FAILURE;
}
/* normalize 'a' so now a is equal to aR */
if ((result = mp_mulmod(&a, &R, &b, &a)) != MP_OKAY) {
  printf("Error computing aR. %s",
          mp_error_to_string(result));
  return EXIT_FAILURE;
}
/* square a to get c = a^2R^2 */
if ((result = mp_sqr(&a, &c)) != MP_OKAY) {
   printf("Error squaring. %s",
          mp_error_to_string(result));
  return EXIT_FAILURE;
/* now reduce 'c' back down to c = a^2R^2 * R^{-1} == a^2R */
if ((result = mp_montgomery_reduce(&c, &b, mp)) != MP_OKAY) {
   printf("Error reducing. %s",
          mp_error_to_string(result));
  return EXIT_FAILURE;
}
/* multiply a to get c = a^3R^2 */
if ((result = mp_mul(&a, &c, &c)) != MP_OKAY) {
  printf("Error reducing. %s",
          mp_error_to_string(result));
  return EXIT_FAILURE;
/* now reduce 'c' back down to c = a^3R^2 * R^{-1} == a^3R */
if ((result = mp_montgomery_reduce(&c, &b, mp)) != MP_OKAY) {
   printf("Error reducing. %s",
          mp_error_to_string(result));
  return EXIT_FAILURE;
}
```

This particular example does not look too efficient but it demonstrates the point of the algorithm. By normalizing the inputs the reduced results are always of the form aR for some variable a. This allows a single final reduction to correct for the normalization and the fast reduction used within the algorithm.

For more details consider examining the file $bn_mp_exptmod_fast.c.$

5.4 Restricted Dimminished Radix

"Dimminished Radix" reduction refers to reduction with respect to moduli that are ameniable to simple digit shifting and small multiplications. In this case the "restricted" variant refers to moduli of the form $\beta^k - p$ for some $k \ge 0$ and $0 where <math>\beta$ is the radix (default to 2^{28}).

As in the case of Montgomery reduction there is a pre-computation phase required for a given modulus.

```
void mp_dr_setup(mp_int *a, mp_digit *d);
```

This computes the value required for the modulus a and stores it in d. This function cannot fail and does not return any error codes. After the precomputation a reduction can be performed with the following.

```
int mp_dr_reduce(mp_int *a, mp_int *b, mp_digit mp);
```

This reduces a in place modulo b with the pre-computed value mp. b must be of a restricted dimminished radix form and a must be in the range $0 \le a < b^2$. Dimminished radix reductions are much faster than both Barrett and Montgomery reductions as they have a much lower asymtotic running time.

Since the moduli are restricted this algorithm is not particularly useful for something like Rabin, RSA or BBS cryptographic purposes. This reduction algorithm is useful for Diffie-Hellman and ECC where fixed primes are acceptable.

Note that unlike Montgomery reduction there is no normalization process. The result of this function is equal to the correct residue.

5.5 Unrestricted Dimminshed Radix

Unrestricted reductions work much like the restricted counterparts except in this case the moduli is of the form $2^k - p$ for 0 . In this sense the unrestricted reductions are more flexible as they can be applied to a wider range of numbers.

```
int mp_reduce_2k_setup(mp_int *a, mp_digit *d);
```

This will compute the required d value for the given moduli a.

```
int mp_reduce_2k(mp_int *a, mp_int *n, mp_digit d);
```

This will reduce a in place modulo n with the pre-computed value d. From my experience this routine is slower than mp_dr_reduce but faster for most moduli sizes than the Montgomery reduction.

Exponentiation

6.1 Single Digit Exponentiation

```
int mp_expt_d (mp_int * a, mp_digit b, mp_int * c)
```

This computes $c=a^b$ using a simple binary left-to-right algorithm. It is faster than repeated multiplications by a for all values of b greater than three.

6.2 Modular Exponentiation

```
int mp_exptmod (mp_int * G, mp_int * X, mp_int * P, mp_int * Y)
```

This computes $Y \equiv G^X \pmod{P}$ using a variable width sliding window algorithm. This function will automatically detect the fastest modular reduction technique to use during the operation. For negative values of X the operation is performed as $Y \equiv (G^{-1} \mod P)^{|X|} \pmod{P}$ provided that gcd(G, P) = 1.

This function is actually a shell around the two internal exponentiation functions. This routine will automatically detect when Barrett, Montgomery, Restricted and Unrestricted Dimminished Radix based exponentiation can be used. Generally moduli of the a "restricted dimminished radix" form lead to the fastest modular exponentiations. Followed by Montgomery and the other two algorithms.

6.3 Root Finding

```
int mp_n_root (mp_int * a, mp_digit b, mp_int * c)
```

This computes $c=a^{1/b}$ such that $c^b \leq a$ and $(c+1)^b > a$. The implementation of this function is not ideal for values of b greater than three. It will work but become very slow. So unless you are working with very small numbers (less than 1000 bits) I'd avoid b>3 situations. Will return a positive root only for even roots and return a root with the sign of the input for odd roots. For example, performing $4^{1/2}$ will return 2 whereas $(-8)^{1/3}$ will return -2.

This algorithm uses the "Newton Approximation" method and will converge on the correct root fairly quickly. Since the algorithm requires raising a to the power of b it is not ideal to attempt to find roots for large values of b. If particularly large roots are required then a factor method could be used instead. For example, $a^{1/16}$ is equivalent to $\left(a^{1/4}\right)^{1/4}$.

Prime Numbers

7.1 Trial Division

int mp_prime_is_divisible (mp_int * a, int *result)

This will attempt to evenly divide a by a list of primes¹ and store the outcome in "result". That is if result = 0 then a is not divisible by the primes, otherwise it is. Note that if the function does not return $\mathbf{MP_OKAY}$ the value in "result" should be considered undefined².

7.2 Fermat Test

```
int mp_prime_fermat (mp_int * a, mp_int * b, int *result)
```

Performs a Fermat primality test to the base b. That is it computes $b^a \mod a$ and tests whether the value is equal to b or not. If the values are equal then a is probably prime and result is set to one. Otherwise result is set to zero.

7.3 Miller-Rabin Test

int mp_prime_miller_rabin (mp_int * a, mp_int * b, int *result)

¹Default is the first 256 primes.

²Currently the default is to set it to zero first.

Performs a Miller-Rabin test to the base b of a. This test is much stronger than the Fermat test and is very hard to fool (besides with Carmichael numbers). If a passes the test (therefore is probably prime) result is set to one. Otherwise result is set to zero.

Note that is suggested that you use the Miller-Rabin test instead of the Fermat test since all of the failures of Miller-Rabin are a subset of the failures of the Fermat test.

7.3.1 Required Number of Tests

Generally to ensure a number is very likely to be prime you have to perform the Miller-Rabin with at least a half-dozen or so unique bases. However, it has been proven that the probability of failure goes down as the size of the input goes up. This is why a simple function has been provided to help out.

```
int mp_prime_rabin_miller_trials(int size)
```

This returns the number of trials required for a 2^{-96} (or lower) probability of failure for a given "size" expressed in bits. This comes in handy specially since larger numbers are slower to test. For example, a 512-bit number would require ten tests whereas a 1024-bit number would only require four tests.

You should always still perform a trial division before a Miller-Rabin test though.

7.4 Primality Testing

```
int mp_prime_is_prime (mp_int * a, int t, int *result)
```

This will perform a trial division followed by t rounds of Miller-Rabin tests on a and store the result in result. If a passes all of the tests result is set to one, otherwise it is set to zero. Note that t is bounded by $1 \le t < PRIME_SIZE$ where $PRIME_SIZE$ is the number of primes in the prime number table (by default this is 256).

7.5 Next Prime

```
int mp_prime_next_prime(mp_int *a, int t, int bbs_style)
```

This finds the next prime after a that passes mp_prime_is_prime() with t tests. Set bbs_style to one if you want only the next prime congruent to $3 \mod 4$, otherwise set it to zero to find any next prime.

7.6 Random Primes

This will find a prime greater than 256^{size} which can be "bbs_style" or not depending on bbs and must pass t rounds of tests. The "ltm_prime_callback" is a typedef for

```
typedef int ltm_prime_callback(unsigned char *dst, int len, void *dat);
```

Which is a function that must read *len* bytes (and return the amount stored) into *dst*. The *dat* variable is simply copied from the original input. It can be used to pass RNG context data to the callback. The function mp_prime_random() is more suitable for generating primes which must be secret (as in the case of RSA) since there is no skew on the least significant bits.

Note: As of v0.30 of the LibTomMath library this function has been deprecated. It is still available but users are encouraged to use the new mp_prime_random_ex() function instead.

7.6.1 Extended Generation

This will generate a prime in a using t tests of the primality testing algorithms. The variable size specifies the bit length of the prime desired. The variable flags specifies one of several options available (see fig. 7.1) which can be OR'ed together. The callback parameters are used as in mp_prime_random().

Flag	Meaning	
LTM_PRIME_BBS	Make the prime congruent to 3 modulo 4	
LTM_PRIME_SAFE	Make a prime p such that $(p-1)/2$ is also prime.	
	This option implies LTM_PRIME_BBS as well.	
LTM_PRIME_2MSB_OFF	Makes sure that the bit adjacent to the most significant bit	
	Is forced to zero.	
LTM_PRIME_2MSB_ON	Makes sure that the bit adjacent to the most significant bit	
	Is forced to one.	

Figure 7.1: Primality Generation Options

Input and Output

8.1 ASCII Conversions

8.1.1 To ASCII

```
int mp_toradix (mp_int * a, char *str, int radix);
```

This still store a in "str" as a base-"radix" string of ASCII chars. This function appends a NUL character to terminate the string. Valid values of "radix" line in the range [2,64]. To determine the size (exact) required by the conversion before storing any data use the following function.

```
int mp_radix_size (mp_int * a, int radix, int *size)
```

This stores in "size" the number of characters (including space for the NUL terminator) required. Upon error this function returns an error code and "size" will be zero.

8.1.2 From ASCII

```
int mp_read_radix (mp_int * a, char *str, int radix);
```

This will read the base-"radix" NUL terminated string from "str" into a. It will stop reading when it reads a character it does not recognize (which happens to include th NUL char... imagine that...). A single leading — sign can be used to denote a negative number.

8.2 Binary Conversions

Converting an mp_int to and from binary is another keen idea.

```
int mp_unsigned_bin_size(mp_int *a);
```

This will return the number of bytes (octets) required to store the unsigned copy of the integer a.

```
int mp_to_unsigned_bin(mp_int *a, unsigned char *b);
```

This will store a into the buffer b in big—endian format. Fortunately this is exactly what DER (or is it ASN?) requires. It does not store the sign of the integer.

```
int mp_read_unsigned_bin(mp_int *a, unsigned char *b, int c);
```

This will read in an unsigned big—endian array of bytes (octets) from b of length c into a. The resulting integer a will always be positive.

For those who acknowledge the existence of negative numbers (heretic!) there are "signed" versions of the previous functions.

```
int mp_signed_bin_size(mp_int *a);
int mp_read_signed_bin(mp_int *a, unsigned char *b, int c);
int mp_to_signed_bin(mp_int *a, unsigned char *b);
```

They operate essentially the same as the unsigned copies except they prefix the data with zero or non–zero byte depending on the sign. If the sign is zpos (e.g. not negative) the prefix is zero, otherwise the prefix is non–zero.

Algebraic Functions

9.1 Extended Euclidean Algorithm

This finds the triple U1/U2/U3 using the Extended Euclidean algorithm such that the following equation holds.

$$a \cdot U1 + b \cdot U2 = U3 \tag{9.1}$$

Any of the U1/U2/U3 paramters can be set to **NULL** if they are not desired.

9.2 Greatest Common Divisor

```
int mp_gcd (mp_int * a, mp_int * b, mp_int * c)
```

This will compute the greatest common divisor of a and b and store it in c.

9.3 Least Common Multiple

```
int mp_lcm (mp_int * a, mp_int * b, mp_int * c)
```

This will compute the least common multiple of a and b and store it in c.

9.4 Jacobi Symbol

```
int mp_jacobi (mp_int * a, mp_int * p, int *c)
```

This will compute the Jacobi symbol for a with respect to p. If p is prime this essentially computes the Legendre symbol. The result is stored in c and can take on one of three values $\{-1,0,1\}$. If p is prime then the result will be -1 when a is not a quadratic residue modulo p. The result will be 0 if a divides p and the result will be 1 if a is a quadratic residue modulo p.

9.5 Modular Inverse

```
int mp_invmod (mp_int * a, mp_int * b, mp_int * c)
```

Computes the multiplicative inverse of a modulo b and stores the result in c such that $ac \equiv 1 \pmod{b}$.

9.6 Single Digit Functions

For those using small numbers $(snicker\ snicker)$ there are several "helper" functions

```
int mp_add_d(mp_int *a, mp_digit b, mp_int *c);
int mp_sub_d(mp_int *a, mp_digit b, mp_int *c);
int mp_mul_d(mp_int *a, mp_digit b, mp_int *c);
int mp_div_d(mp_int *a, mp_digit b, mp_int *c, mp_digit *d);
int mp_mod_d(mp_int *a, mp_digit b, mp_digit *c);
```

These work like the full mp_int capable variants except the second parameter b is a mp_digit. These functions fairly handy if you have to work with relatively small numbers since you will not have to allocate an entire mp_int to store a number like 1 or 2.

Index

mp_add, 29	mp_invmod, 52
mp_add_d , 52	mp_jacobi, 52
mp_and, 29	mp_lcm, 51
mp_clear, 11	mp_lshd, 28
mp_clear_multi, 12	MP_LT, 22
mp_cmp, 24	$MP_MEM, 9$
mp_cmp_d, 25	$mp_mod, 35$
mp_cmp_mag, 23	$mp_mod_d, 52$
$mp_div, 30$	mp_montgomery_calc_normalization,
mp_div_2, 26	38
mp_div_2d, 28	mp_montgomery_reduce, 37
mp_div_d , 52	mp_montgomery_setup, 37
mp_dr_reduce, 40	mp_mul, 31
mp_dr_setup, 40	mp_mul_2, 26
MP_EQ, 22	mp_mul_2d, 28
mp_error_to_string, 10	mp_mul_d, 52
mp_expt_d , 43	mp_n_root, 44
mp_exptmod, 43	mp_neg, 29
mp_exteuclid, 51	MP_NO, 9
mp_gcd, 51	MP_OKAY, 9
mp_get_int, 20	mp_or, 29
mp_grow, 16	mp_prime_fermat, 45
$MP_{-}GT$, 22	mp_prime_is_divisible, 45
mp_init, 11	mp_prime_is_prime, 46
mp_init_copy, 13	mp_prime_miller_rabin, 45
mp_init_multi, 12	mp_prime_next_prime, 46
mp_init_set, 21	mp_prime_rabin_miller_trials, 46
mp_init_set_int, 21	mp_prime_random, 47
mp_init_size, 14	mp_prime_random_ex, 47
mp_int, 10	mp_radix_size, 49

54 INDEX

mp_read_radix, 49 mp_read_unsigned_bin, 50 mp_reduce, 36 mp_reduce_2k, 41 mp_reduce_2k_setup, 41 mp_reduce_setup, 36 $mp_rshd, 28$ mp_set, 19 mp_set_int, 20 $mp_shrink, 15$ mp_sqr, 33 mp_sub, 29 $mp_sub_d, 52$ $mp_to_unsigned_bin, \, 50$ mp_toradix, 49 mp_unsigned_bin_size, 50 MP_VAL, 9 mp_xor, 29 MP_YES, 9